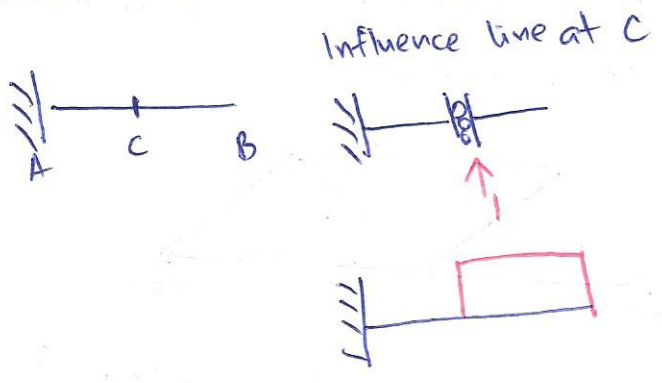


3/12/2015

Previously, we stop at Müller-Breslau method, where we apply a vertical roller to construct influence line.

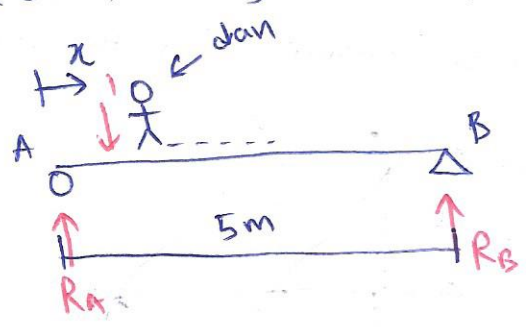


Why only 1 unit load?

Here, the application of (I.L) can determine

- 1) reaction force
  - 2) shear force
  - 3) bending moment
- using I.L, we can determine all this at the specific point.

How about a load of 590 N of (dan) along the span?



$$\sum F_y = 0$$

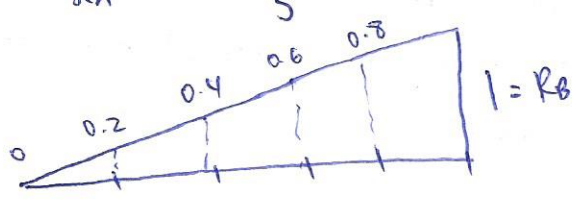
$$R_A + R_B = 1$$

$$\sum M_A = 0$$

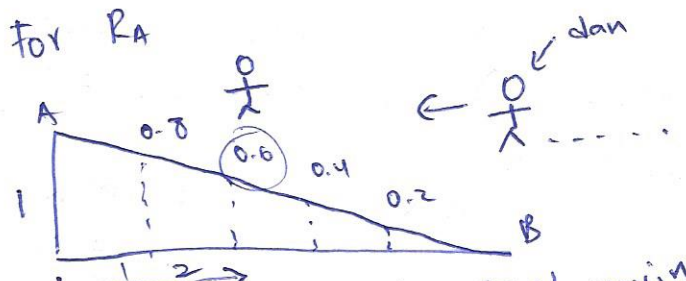
$$1 \cdot x - R_B \cdot 5 = 0$$

$$R_B = \frac{x}{5}$$

$$R_A = 1 - \frac{x}{5}$$



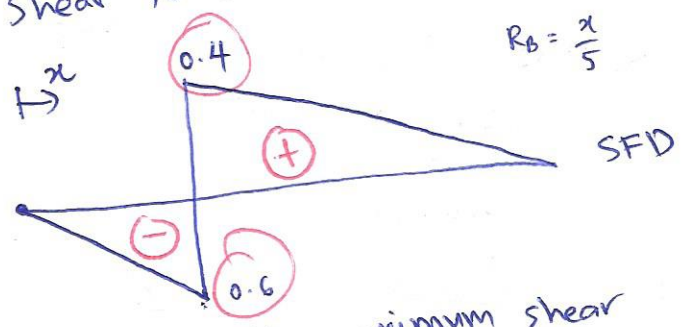
for RA  
if a moving load of 590 N moving from B → A, specifically at point 0.6, so the influence line should be?



Shear Force

$$R_A = 1 - \frac{x}{5}$$

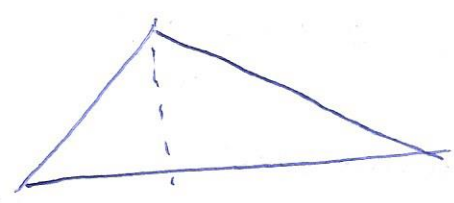
$$R_B = \frac{x}{5}$$



when  $x = 2$ , the maximum shear force  $590 \times 0.4 = 236 \text{ N}$

also, at  $x = 2$ , there is the minimum shear force  $590 \times (-0.6) = -354 \text{ N}$

Then, the maximum bending moment



$$0 \leq x \leq 2$$

$$2 \leq x \leq 5$$

$$M_x = -2 + 2x - \frac{x^2}{5}$$

$$M_x = 6 - \frac{6}{5}x$$

$$M_x = x - \frac{x^2}{5}$$

when  $x = 2$

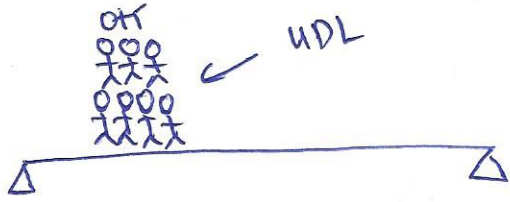
$$M_x = -2 + 4 - \frac{4}{5}$$

$$= 1.2 \text{ kNm}$$

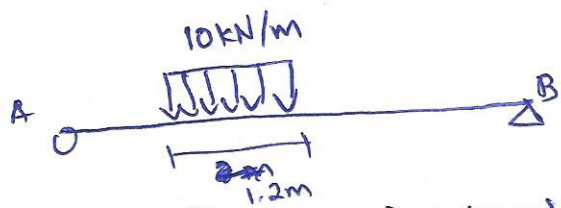
So, the maximum bending moment when (dm) is at 2m from A should be

$$590 \times 1.2 = 708 \text{ Nm}$$

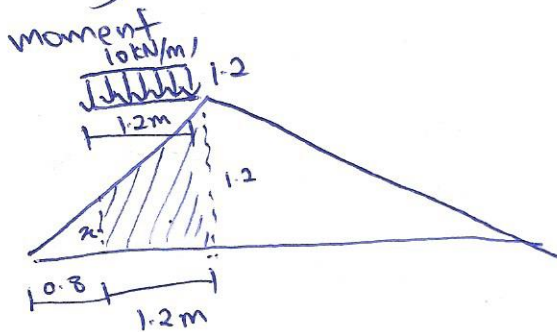
Aaaa... that's for a ~~unit~~ point load



\* The really concern is the bending moment!



Using the I.L for bending



$$\frac{0.8}{x} = \frac{2}{1.2} \Rightarrow x = \frac{0.8 \times 1.2}{2} = 0.48$$

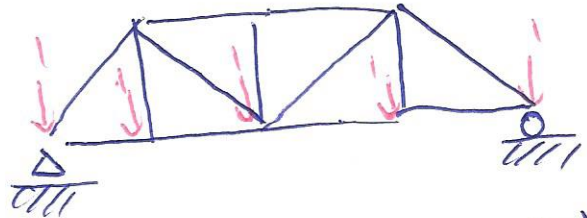
So, the trapezium area is

$$M_x = \frac{1}{2} (1.2 + 0.48) \times 1.2 \times 10 = \underline{\underline{10.08 \text{ kNm}}}$$

\* The total moment influence line when all guys (10 kN/m) is at 2m from A.

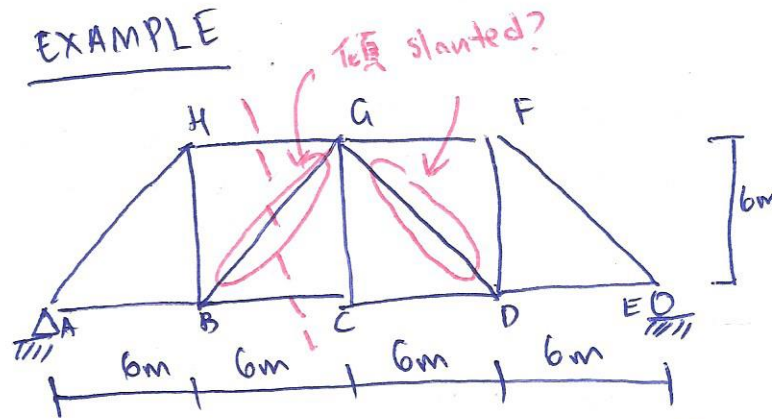
## Influence line for truss

When determining the I-L for truss, normally we use method of section.

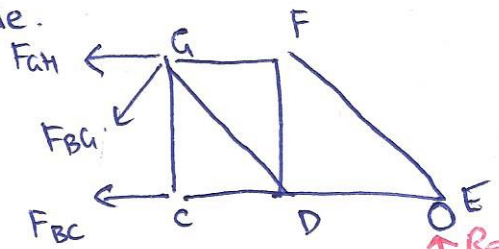


\* the 1 unit load is applied at the joint or the support.

### EXAMPLE



Let say we consider from the right side.



Firstly, don't apply any load to achieve the equilibrium condition

$$\sum F_x = 0$$

$$\sum F_y = 0$$

$$F_{GH} = 0$$

$$R_E - F_{BG} \sin 45^\circ = 0$$

$$F_{BC} = 0$$

$$\underline{\underline{R_E = F_{BG} \sin 45^\circ}}$$

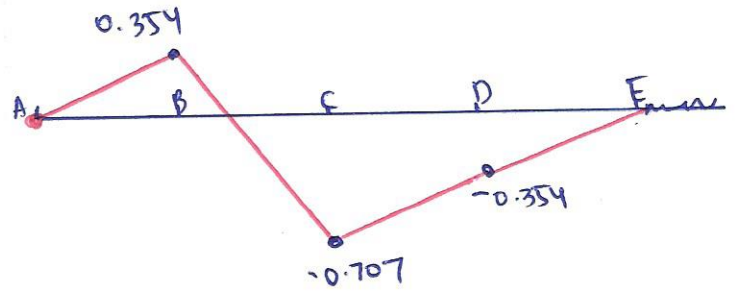
Then, ~~for~~ for truss case, apply a beam to construct the influence line.

At B, when  $x=6$

$$R_E = F_{BC} \sin 45^\circ$$

$$F_{BC} = \frac{R_E}{\sin 45^\circ} = \frac{0.25}{\sin 45^\circ} = 0.354 \quad *$$

Now, construct the influence line!

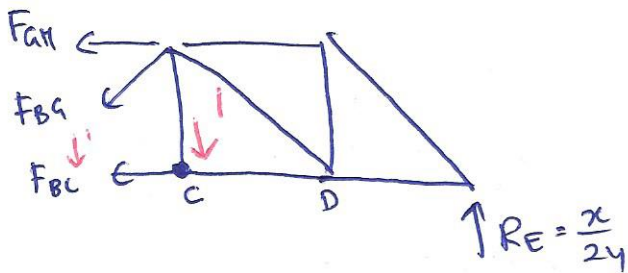


At C, when  $x=12$

$$R_E = F_{BC} \sin 45^\circ$$

$$F_{BC} = \frac{R_E}{\sin 45^\circ} = \frac{0.5}{\sin 45^\circ} = 0.71$$

But why?



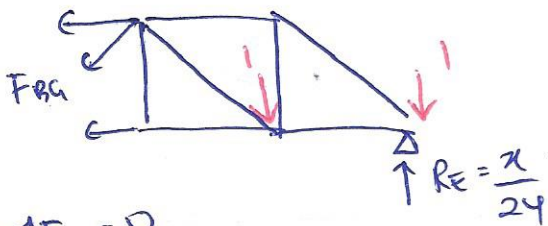
At C, when  $x=12$

$$\sum F_y = 0$$

$$F_{BC} \sin 45^\circ + 1 = R_E \quad -0.707$$

$$F_{BC} = \frac{R_E - 1}{\sin 45^\circ} = \frac{0.5 - 1}{\sin 45^\circ} = -0.71$$

At D, when  $x=18$



$$\sum F_y = 0$$

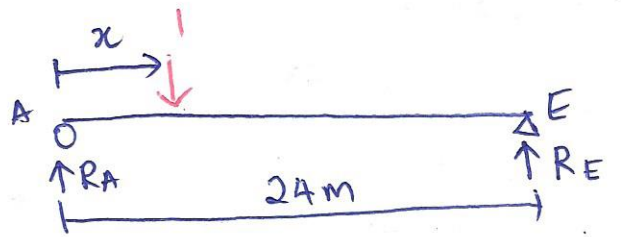
$$F_{BC} \sin 45^\circ + 1 = R_E$$

$$F_{BC} = \frac{R_E - 1}{\sin 45^\circ} = \frac{0.75 - 1}{\sin 45^\circ} = -0.354$$

At E when  $x=24$

$$F_{BC} \sin 45^\circ + 1 = R_E$$

$$F_{BC} = \frac{R_E - 1}{\sin 45^\circ} = \frac{1 - 1}{\sin 45^\circ} = 0$$



$$\sum F_y = 0$$

$$R_A + R_E = 1$$

$$\sum M_A = 0$$

$$1 \cdot x - R_E \cdot 24 = 0$$

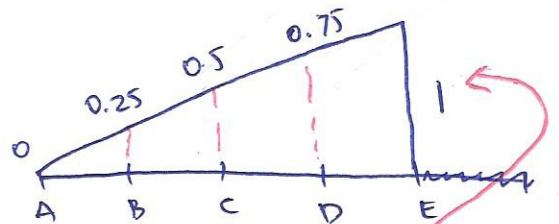
$$1 \cdot x - R_E \cdot 24 = 0$$

$$R_E = \frac{x}{24}$$

$$R_A = 1 - R_E = 1 - \frac{x}{24}$$

Then, plot it!

Joint	Distance	$R_E = \frac{x}{24}$
A	0	0
B	6	0.25
C	12	0.5
D	18	0.75
E	24	1



So, using the value of the influence line for beam, plot it for the truss.

At A, when  $x=0$

$$R_E = F_{BG} \sin 45^\circ$$

We want to determine the  $F_{BG}$

$$F_{BG} = \frac{R_E}{\sin 45^\circ} = \frac{0}{\sin 45^\circ} = 0 \text{ N}$$